

## Key

## LESSON 16.2

*For use with pages 420–427*

~~★~~only do circled problems

$$256 = 2^8$$

rational exponents.

1.  $64^{2/3} =$   
 $(64^{1/3})^2 = 4^2 = 16$

$$\textcircled{2} \quad 8^{-3/4} = \frac{1}{8^{3/4}}$$

3.  $\sqrt[6]{256} =$

$$\sqrt[6]{2^8} = \sqrt[6]{2^6 \cdot 2^2}$$

4.  $5\frac{1}{4} \cdot 3\frac{1}{4}$

5.  $\sqrt[4]{2} \cdot \sqrt[4]{8}$

6.  $\frac{\sqrt[4]{192}}{\sqrt[4]{6}} = 2\sqrt[6]{2^2} = 2\sqrt[6]{4}$

Handwritten diagram illustrating the binary tree structure for the expression  $64 \div 4$ :

```

      64 \ 4
     /  \
    8    8  (2)(2)
   /  \
  (2)(4)(2)(4)
 /  \ /  \
(2)(2)(2)(2)

```

$$\sqrt[3]{54} = \sqrt[3]{27} \sqrt[3]{2} = 3\sqrt[3]{2}$$

7.  $\frac{11}{\sqrt[4]{11}}$

8.  $\sqrt[3]{7} \cdot \sqrt[3]{49} =$  9.  $\sqrt[3]{7 \cdot 49} = \sqrt[3]{343} = \boxed{7}$

9.  $(3^{3/2})^2$

$$\frac{54^{1/3}}{4} = \frac{3\sqrt[3]{2}}{4} = \frac{3(2)^{1/3}}{4}$$

11.  $\frac{\sqrt[4]{32}}{\sqrt{2}} = \sqrt[4]{\frac{32}{2}}$   
 $\sqrt[4]{16} = \boxed{2}$

$$12. \frac{\sqrt[5]{5}}{\sqrt[5]{27}} \cdot \frac{\sqrt[5]{9}}{\sqrt[5]{9}} = \frac{\sqrt[5]{45}}{\sqrt[5]{243}} = \boxed{\frac{\sqrt[5]{45}}{3}}$$

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13.  $x^{5/3} \cdot x^{4/3}$

14.  $\sqrt{x^{2/5}}$

15.  $(x^{1/2})^{2/7}$

16.  $\left(\frac{x^{2/3}}{27}\right)^{3/4} = \frac{x^{2/3}}{27^{1/3}} = 17. \sqrt[3]{16x^4}$

18.  $(x^{-3})^{2/5}$

$$\sqrt[3]{64x^3y} = 4x\sqrt[3]{y}$$

19.  $\frac{x^{7/5}}{x^{4/5}}$

$$\frac{4}{4} = 1$$

20.  $\frac{\sqrt[3]{64x^3y}}{4x^{-3}y} = \frac{(4x^3y)^{\frac{1}{3}}}{4x^{-3}y} = \frac{4^{\frac{1}{3}}x^1y^{\frac{1}{3}}}{4x^{-3}y} = \frac{4^{\frac{1}{3}}x^1y^{\frac{1}{3}}}{4^1x^{-3}y^1} = 4^{\frac{1}{3}-1}x^{1-(-3)}y^{\frac{1}{3}-1} = 4^{-\frac{2}{3}}x^4y^{-\frac{2}{3}} = \frac{1}{4^{\frac{2}{3}}}x^4y^{-\frac{2}{3}} = \frac{1}{4\sqrt[3]{4}}x^4y^{-\frac{2}{3}} = \frac{1}{4\sqrt[3]{4}}x^4y^{-\frac{2}{3}}$

$$x^5 \cdot x^{\sqrt{2}}$$

can leave  
because radical is in  
numerator.

22.  $(x^{\sqrt{2}})^{3\sqrt{2}}$

23.  $\frac{x^{4\sqrt{3}}}{2x^{2\sqrt{3}}}$

24.  $(\sqrt[3]{x^4} \cdot \sqrt{x^5})^{-2} =$

$$\left(\frac{2}{2}\right) \frac{4}{3} + \frac{5}{2} \left(\frac{3}{3}\right) =$$

$$\frac{8}{6} + \frac{15}{6} = \frac{23}{6}$$

$$(X^{4/3} \cdot X^{5/2})^{-2} = X^{-46/6}$$

$$X^{-23/3} = \frac{1}{X^{23/3}} = \frac{1}{X^7 X^{2/3}} \cdot \frac{X^{1/3}}{X^{1/3}} =$$

$$\frac{X^{1/3}}{X^7 \cdot X^{3/3}} = \frac{X^{1/3}}{X^7 \cdot X} = \frac{X^{1/3}}{X^8}$$

$$\sqrt{27} = \sqrt{9 \cdot 3} = 3\sqrt{3}$$

$$\sqrt{48} = \sqrt{16 \cdot 3} = 4\sqrt{3}$$

Name \_\_\_\_\_

Date \_\_\_\_\_

LESSON  
6.2

# Practice continued

For use with pages 420-427

Perform the indicated operation. Assume all variables are positive.

25.  $6\sqrt[3]{5} + 2\sqrt[3]{5}$

26.  $5\sqrt{5} - \sqrt{45}$

27.  $2\sqrt{27} - 3\sqrt{48}$

28.  $2\sqrt{x} + 7\sqrt{x}$

$$2(3\sqrt{3}) - 3(4\sqrt{3}) = 6\sqrt{3} - 12\sqrt{3} = \boxed{-6\sqrt{3}}$$

29.  $3(x^{1/2}y^3)^2 - (x^3y^{18})^{1/3}$

30.  $4x^{1/3} + x^{1/3}$

$$3(x^{2/2}y^6) - x^{3/3}y^{18/3} = 3xy^6 - xy^6 = \boxed{2xy^6}$$

Write the expression in simplest form. Assume all variables are positive.

31.  $\sqrt[4]{3x^7y^9z^3}$

32.  $\sqrt{x^3y^4z} \cdot \sqrt{xyz^4}$

33.  $\sqrt[3]{\frac{81x}{8yz}}$

$$\sqrt[3]{\frac{81x}{8yz}} = \sqrt[3]{\frac{81x}{8yz}}$$

$$\sqrt[4]{3x^4x^3y^4y^4yz^3} = x \cdot y \cdot y \cdot \sqrt[4]{3x^3yz^3} = \boxed{xy^2\sqrt[4]{3x^3yz^3}}$$

Solve for x and simplify.

34.  $X^3 + 17 = 137$

$$\sqrt[3]{X^3} = \sqrt[3]{120} \quad X = \sqrt[3]{120}$$

$$\boxed{X = 2\sqrt[3]{15}}$$

35.  $\frac{2(X-1)^4}{2} = \frac{162}{2}$

$$\sqrt[4]{(X-1)^4} = \sqrt[4]{81}$$

$$X-1 = \pm 3$$

$$X-1 = 3 \quad + \quad X-1 = -3$$

$$\boxed{X = 4 \quad + \quad X = -2}$$

$$x^{2-1} = x \quad y^{3-4} = y^{-1} = \frac{1}{y} \quad \sqrt[3]{\frac{81x}{8yz}} = \frac{\sqrt[3]{81x}}{2\sqrt[3]{yz}}$$

$$\frac{\sqrt[3]{81x}}{2\sqrt[3]{yz}} \cdot \frac{\sqrt[3]{y^2z^2}}{\sqrt[3]{y^2z^2}} = \frac{\sqrt[3]{81xy^2z^2}}{2\sqrt[3]{y^3z^3}}$$

$$\frac{\sqrt[3]{81xy^2z^2}}{2\sqrt[3]{y^3z^3}} = \frac{\sqrt[3]{81xy^2z^2}}{2yz}$$

$$\sqrt[3]{81} = 3\sqrt[3]{27} = 3\sqrt[3]{3}$$

$$\boxed{\frac{3\sqrt[3]{3xy^2z^2}}{2yz}}$$