

A **quadratic inequality in two variables** can be written in one of the following forms:

$$y < ax^2 + bx + c$$

$$y \leq ax^2 + bx + c$$

$$y > ax^2 + bx + c$$

$$y \geq ax^2 + bx + c$$

To graph a quadratic inequality in one of the forms above, follow these steps:

**Step 1: Graph** the parabola  $y = ax^2 + bx + c$ . Make the parabola *dashed* for inequalities with  $<$  or  $>$  (not equal to) and *solid* for inequalities with  $\leq$  or  $\geq$  (equal to).

**Step 2: Test** a point  $(x, y)$  to determine whether the point is a solution of the inequality. Remember the point you test cannot be on the parabola itself.

**Step 3: Shade** the region using the point you tested in Step 2. If the point produces a true statement, then you shade where the point is. If the point produces a false statement, then you shade where the point is not.

**Example:** Graph  $y > x^2 + 3x - 4$ .

**Step 1: Graph**  $y = x^2 + 3x - 4$ . Since the inequality symbol is  $>$ , make the parabola dashed.

**Step 2: Test** a point, such as  $(0, 0)$ .

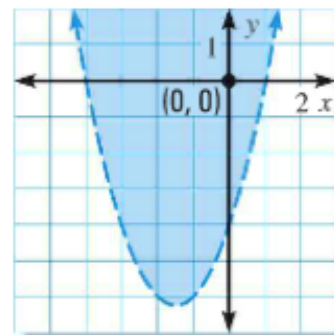
$$y > x^2 + 3x - 4$$

$$0 > (0)^2 + 3(0) - 4$$

$$0 > -4 \quad \checkmark$$

So,  $(0,0)$  is a solution of the inequality.

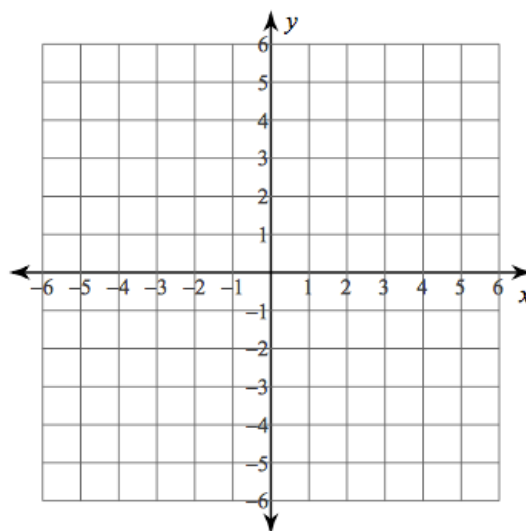
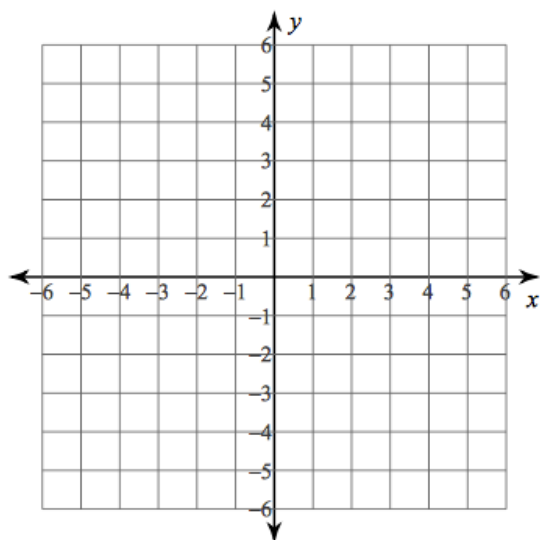
**Step 3: Shade** the region of the parabola where  $(0, 0)$  is (inside the parabola).



Graph the following quadratic inequalities on a coordinate plane.

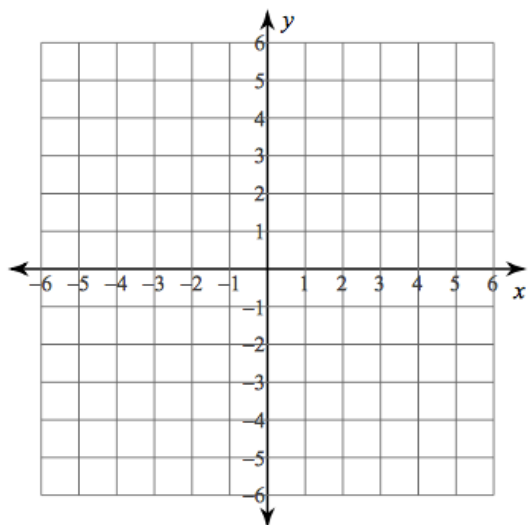
1)  $y \geq x^2 + 2x - 3$

2)  $y < -x^2 + 4x - 3$

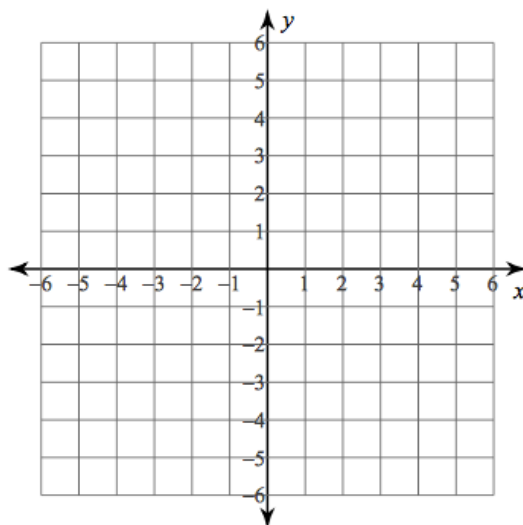


Graph the following system of quadratic inequalities on a coordinate plane. Remember, it is helpful just to use arrows at first and then shade your final solution. You may need to change the units of your axes.

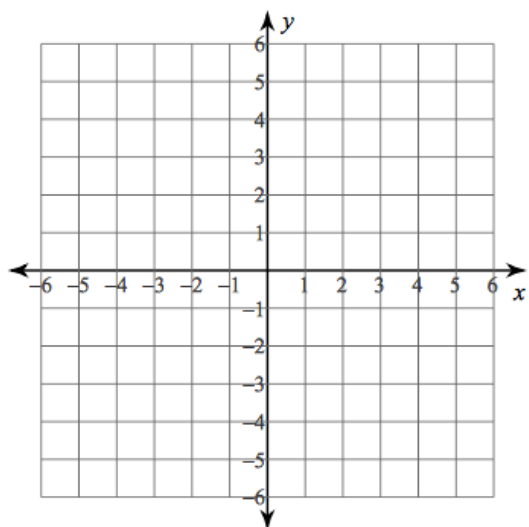
3)  $y \leq -x^2 + 4$   
 $y > x^2 - 2x - 3$



4)  $y \geq 2x^2$   
 $y < -x^2 + 1$



5)  $y \leq -x^2 + 4x - 4$   
 $y < 2x^2 + x - 8$



$y \geq x^2 - x - 6$   
6)  $y < -2x^2 - 4x + 3$   
 $y \geq x$

