

1) What is the equation for the axis of symmetry of a quadratic function (in all forms)? What else can you find using the axis of symmetry? (4.1) → x-coordinate of the vertex

Standard form:

$$y = ax^2 + bx + c$$

Vertex form:

$$y = a(x-h)^2 + k \quad (h, k)$$

vertex:

$$X = h$$

Intercept (factored) form:

$$y = a(x-p)(x-q)$$

$$X = \frac{p+q}{2}$$

Factor the following expressions: (4.3/4.4)

2) $w^2 - 8w + 12$

$$(w-6)(w-2)$$

3) $x^2 - 16$ difference of two squares

$$(x-4)(x+4)$$

4) $x^2 + 3x - 28$

$$(x+7)(x-4)$$

5) $3z^3 - 15z^2 + 36z$

GCF

$$3z(z^2 - 5z + 12)$$

$$\begin{array}{r|l} 12 & -5 \\ -6 & -2 \end{array}$$

prime

6) $18x^2 - 32$

GCF

$$2(9x^2 - 16)$$

$$2(3x+4)(3x-4)$$

7) $3w^2 - 11w - 4$

$$\begin{array}{r|l} -4 & 3 \\ -12 & 1 \end{array} \rightarrow \begin{array}{l} \downarrow \quad \downarrow \quad \downarrow \\ (3w^2 - 12w) + (w - 4) = \\ 3w(w-4) + 1(w-4) = \\ (3w+1)(w-4) \end{array}$$

Solve the following equations by factoring. (4.3/4.4)

8) $9x^2 - 3x = 0$

GCF

$$3x(3x-1) = 0$$

$$3x = 0 \quad \text{or} \quad 3x-1 = 0$$

$$x = 0 \quad \text{or} \quad x = \frac{1}{3}$$

9) $7w^2 + 28w = 0$

GCF

$$7w(w+4) = 0$$

$$7w = 0 \quad \text{or} \quad w+4 = 0$$

$$w = 0 \quad \text{or} \quad w = -4$$

10) $144 = 25x^2$

$$-144 \quad -144$$

$$25x^2 - 144 = 0$$

$$(5x+12)(5x-12) = 0$$

$$5x+12=0 \quad \text{or} \quad 5x-12=0$$

$$5x = -12 \quad \text{or} \quad 5x = 12$$

$$x = -12/5 \quad \text{or} \quad x = 12/5$$

11) $25 = x^2 - 8x + 16$

$$-25 \quad -25$$

$$x^2 - 8x - 9 = 0$$

$$(x-9)(x+1) = 0$$

$$x-9=0 \quad \text{or} \quad x+1=0$$

$$x = 9 \quad \text{or} \quad x = -1$$

12) $12x^2 + 5x + 5 = 7$

$$-7 \quad -7$$

$$12x^2 + 5x - 2 = 0$$

$$(12x^2 + 8x) + (-3x - 2) = 0$$

$$4x(3x+2) - 1(3x+2) = 0$$

$$(4x-1)(3x+2) = 0$$

$$4x-1=0 \quad \text{or} \quad 3x+2=0$$

$$4x = \frac{1}{4} \quad \text{or} \quad 3x = -\frac{2}{3}$$

$$x = \frac{1}{4} \quad \text{or} \quad x = -\frac{2}{3}$$

Solve the following equations by using square roots. (4.5)

13) $4x^2 + 100 = 0$

$$-100 \quad -100$$

$$\frac{4x^2}{4} = \frac{-100}{4}$$

$$\sqrt{x^2} = \sqrt{-25}$$

$$x = \pm \sqrt{-25}$$

$$x = \pm 5i$$

opposite of

G.E.M.S.

SO

S.M.E.G.

$$\begin{array}{c} \sqrt{-25} \\ \downarrow \quad \downarrow \\ \sqrt{-1} \quad \sqrt{25} \\ i \quad 5 \end{array}$$

14) $25 = 7b^2 - 10$

$$+10 \quad +10$$

$$\frac{35}{7} = \frac{7b^2}{7}$$

$$\sqrt{5} = \sqrt{b^2}$$

$$b = \pm \sqrt{5}$$

Write the following expressions as a complex number in standard form. (4.6)

15) $(2 - 5i) + (-1 - 3i)$
 $2 - 5i - 1 - 3i =$
 $\boxed{1 - 8i}$

16) $(2 - 5i) - (-1 - 3i)$
 $2 - 5i + 1 + 3i =$
 $\boxed{3 - 2i}$

multiply by conjugate FOIL
 $17) \frac{(2-3i)(4-i)}{(4+i)(4-i)} \quad i^2 = -1$
 $\frac{8-12i-2i+3i^2}{16-4i^2+4i-i^2} =$
 $\frac{8-14i-3}{16+1} = \frac{5-14i}{17}$

18) If $(ax + 2)(3x - 5b) - bx^2 = -11x^2 + 36x - 20$, what is the value of $a + b$? (4.3/4.4)
 $3ax^2 - 5abx + 6x - 10b - bx^2 = -11x^2 + 36x - 20$
 \hookrightarrow constant term (no x)
 $-10b = -20 \quad b = 2$
 Quadratic terms:
 $3ax^2 - bx^2 = -11x^2$
 $3ax^2 - 2x^2 = -11x^2$
 $a = -3$
 $a + b = 2 + (-3) = \boxed{-1}$

19) Write a quadratic function in vertex form with the vertex $(-1, -4)$ and passes through the point $(2, -1)$. How has this graph shifted from the original quadratic parent function? (4.10)

$y = a(x-h)^2 + k$ vertex: (h, k)
 $y = a(x+1)^2 - 4$
 $-1 = a(2+1)^2 - 4$
 $-1 = 9a - 4$
 $3 = 9a$
 $a = 3/9 = 1/3$
 $y = \frac{1}{3}(x+1)^2 - 4$
 graph is shifted to the left one and down four from parent function (look at vertex)

Simplify the following expressions. (4.5)

20) $\sqrt{10} \cdot \sqrt{15} = \sqrt{150} = \sqrt{25 \cdot 6} =$
 $\sqrt{25} \cdot \sqrt{6} = 5\sqrt{6}$

22) $\sqrt{\frac{5}{2}} = \frac{\sqrt{5}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{10}}{\sqrt{4}} = \frac{\sqrt{10}}{2}$

21) $\frac{2(6+\sqrt{8})}{6-\sqrt{8}(6+\sqrt{8})}$
 multiply by conjugate
 $\frac{12+2\sqrt{8}}{36+6\sqrt{8}-6\sqrt{8}-\sqrt{64}} = \frac{12+2\sqrt{8}}{36-8} = \frac{12+2\sqrt{8}}{28} =$
 $\frac{12+4\sqrt{2}}{28} = \frac{3+\sqrt{2}}{7}$

Solve the using the quadratic formula. (4.8)

23) $y = x^2 + 6x + 4$
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $x = \frac{-6 \pm \sqrt{(6)^2 - 4(1)(4)}}{2(1)}$
 $= \frac{-6 \pm \sqrt{36-16}}{2}$
 $= \frac{-6 \pm \sqrt{20}}{2} = \frac{-6 \pm 2\sqrt{5}}{2} = \boxed{-3 \pm \sqrt{5}}$

24) $y = 2x^2 - 16x + 50$
 $x = \frac{-(-16) \pm \sqrt{(-16)^2 - 4(2)(50)}}{2(2)} = \frac{16 \pm \sqrt{256-400}}{4} =$
 $\frac{16 \pm \sqrt{-144}}{4} = \frac{16 \pm 12i}{4} = \boxed{4 \pm 3i}$

Solve the inequality algebraically, write the solution in interval notation. (4.9)

25) $x^2 + 2x - 3 > 0$
 $x^2 + 2x - 3 = 0$
 $(x+3)(x-1) = 0$
 $x+3=0$ or $x-1=0$
 $x=-3$ or $x=1$
 Test $x=0$:
 $0^2 + 2(0) - 3 > 0$
 $-3 > 0$ NO
 $\boxed{(-\infty, -3) \cup (1, \infty)}$

26) $x^2 - 3x \leq 10$
 $x^2 - 3x - 10 \leq 0$
 $(x-5)(x+2) = 0$
 $x-5=0$ or $x+2=0$
 $x=5$ or $x=-2$
 Test $x=0$:
 $0^2 - 3(0) \leq 10$
 $0 \leq 10$ Yes
 $\boxed{[-2, 5]}$